Normalized solutions of Schrödinger equations on domains

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Abstract: The existence of solutions $(\lambda, u) \in \mathbb{R} \times H_0^1(\Omega)$ of nonlinear Schrödinger equations like

(1)
$$-\Delta u + V(x)u + \lambda u = f(u) \quad \text{in } \Omega \subset \mathbb{R}^N$$

with prescribed L^2 -norm

(2)
$$\int_{\Omega} u^2 = a$$

has found considerable interest in the last decade. If $\Omega = \mathbb{R}^N$ and *V* is constant then the scaling $s * u(x) = s^{N/2}u(sx)$ plays an important role in proving the Palais-Smale condition for the associated functional on the L^2 -sphere. We present recent results on the existence of solutions of (1)-(2) on bounded domains where this scaling cannot be used.

The talk is based on work with Shijie Qi and Wenming Zou.